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# Comparative theoretical study of [3+2] and [2+2] cycloadditions of ethylene and WXYMe<sub>2</sub>; *X*, *Y* = (=O), (=NH), (=CH<sub>2</sub>)<sup> $\Leftrightarrow$ </sup>

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# ABSTRACT

Quantum chemical calculations employing density functional theory (B3LYP) were carried out to compare the preference of [3+2] versus [2+2] cycloadditions of ethylene to  $WO_2(CH_3)_2$  (**W2**),  $WONH(CH_3)_2$ (**W3**),  $WNHCH_2(CH_3)_2$  (**W4**),  $W(CH_2)_2(CH_3)_2$  (**W5**), and  $W(NH)_2(CH_3)_2$  (**W6**). The results are compared to previously published data on the related tungsten complex  $WOCH_2(CH_3)_2$  (**W1**). In agreement with  $MoOCH_2(CH_3)_2$  and  $ReO_2CH_3CH_2$ , all six tungsten complexes prefer a [2+2] pathway rather than a [3+2] cycloaddition which is the reverted preference compared to the analogous compounds  $TcO_2CH_3CH_2$ ,  $MnO_2CH_3CH_2$ ,  $RuO_3CH_2$ ,  $OsO_3CH_2$  and  $OsO_2(NH)_2$ , and  $MO_2CH_3CH_2$  (**W** = Ir, Rh, Co).

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## 1. Introduction

The mechanism of the *cis*-dihydroxylation of olefins with OsO<sub>4</sub> is now well established after a controversy about two alternative pathways was finally solved with the help of quantum chemical investigations. Originally, a concerted [3+2] cycloaddition was proposed [1] while an alternative two-step pathway with initial [2+2] addition with subsequent rearrangement was later suggested [2]. Both pathways yield an osma-2,5-dioxolane as final product. It was shown that the initial [2+2] cycloaddition has a significantly higher barrier than the [3+2] pathway [3]. Other metal oxides like RuO<sub>4</sub> and ReO<sub>4</sub><sup>--</sup> were also predicted to prefer a [3+2] cycloaddition rather than a [2+2] reaction [4,5]. A study by Deubel and Muñiz showed that the pathway via [3+2] cycloaddition is still preferred for ethylene addition to OsO<sub>2</sub>(NH)<sub>2</sub> [6]. The authors predicted a decrease of the activation energies in the order O/O > O/NH > NH/NH.

A different scenario is theoretically predicted when a metalcarbon double bond is involved: the [2+2] addition of ethylene across the M=C alkylidene bond becomes competitive with the [3+2] reaction for  $OsO_3CH_2$  and  $OsO_2(CH_2)_2$  [7,8] and the former reaction becomes favored over the latter for  $ReO_2CH_3CH_2$  [9],  $WO(CH_3)_2CH_2$ ,  $MOO(CH_3)_2CH_2$ , and  $CrO(CH_3)_2CH_2$  [10]. The [3+2] cycloaddition of ethylene is preferred for  $TcO_2CH_3CH_2$  [11],

RuO<sub>3</sub>CH<sub>2</sub> [12], IrO<sub>2</sub>CH<sub>3</sub>CH<sub>2</sub>, RhO<sub>2</sub>CH<sub>3</sub>CH<sub>2</sub>, and CoO<sub>2</sub>CH<sub>3</sub>CH<sub>2</sub> [13]. Experimentally, Schrock reported the synthesis of RR'W(=NAr) (=CHCMe<sub>3</sub>) and he showed that the reaction of the latter with ethylene yields RR'W(=NAr)(=CH<sub>2</sub>) and H<sub>2</sub>C=CHCMe<sub>3</sub> which indicates that a [2+2] addition across the W=CHCMe<sub>3</sub> double bond has taken place [14]. As part of our ongoing theoretical work about the reaction mechanism of olefin addition to metal=E double bonds [3a,4a,b,5,7-13] we present a comparative study of [2+2] and [3+2] ethylene additions to  $W(=O)_2(CH_3)_2$  (W2),  $(O=)W(=NH)(CH_3)_2$  (W3),  $(H_2C=)W(=NH)(CH_3)_2$  (W4),  $(H_2C=)$  $W(=CH_2)(CH_3)_2$  (W5) and  $(HN=)W(=NH)(CH_3)_2$  (W6). We compare the results with our previously published data for the ethylene addition to  $(O=)W(=CH_2)(CH_3)_2$  (W1) [10a], its lighter homologs [10b], and similar group-7 [9,11], group-8 [7,8,12], and group-9 [13] compounds. Due to the diversity of the compounds, we only consider [3+2] and [2+2] pathways. Therefore, we can not exclude that other pathways play an important role for ethylene addition to these complexes. The aim of this work is to elucidate the preference of the metal compounds for a [3+2] or a [2+2] addition reaction.

# 2. Methods

All geometry optimizations were carried out using hybrid density functional theory (DFT) employing the B3LYP hybrid functional [15] as implemented [16] in the GAUSSIAN 03 program [17] without any symmetry constraints. Ahlrichs' triple zeta basis set (TZVP) [18] was used for the elements O, N, C and H. For tungsten, the Stuttgart/Köln relativistic effective core potential (ECP) replacing

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60 core electrons was employed in combination with a (311111/ 22111/411) [19] valence basis set. This combination is denoted as basis set I. Analytical vibrational harmonic frequencies were calculated at all stationary points to verify their nature (minimum, transition state or higher order saddlepoint). Intrinsic reaction coordinate (IRC) [20] calculations were carried out to ensure the connectivity of the minima and transition states. Additional B3LYP single point energies were computed at all transition states and minima with a larger basis set denoted as basis set II. There, the correlation consistent triple zeta basis sets of Dunning (ccpVTZ) [21] were used for the elements O, N, C and H. The tungsten basis set is augmented by two sets of *f* and one set of *g* functions derived by Martin and Sundermann [22]. All energies discussed in this study relate to B3LYP/II//B3LYP/I and are corrected by the unscaled zero point energy (ZPE) contributions obtained at B3LYP/I unless otherwise stated. This is consistent and directly comparable with our previously published data.

### 3. Results and discussion

The focus of this work lies on the energetics of the [2+2] and [3+2] cycloadditions rather than the geometries of the compounds. Therefore, we discuss only the reaction energies and activation barriers but not the geometries of the calculated species. A full set of cartesian coordinates and energies of all compounds is given as Supporting information.

Fig. 1 shows the possible [3+2] and [2+2] cycloadditions. On the right hand side of Fig. 1, the [2+2] cycloaddition **W2** +  $C_2H_4 \rightarrow$  **W2-1** with a rather high barrier is shown. The highly endothermic [3+2] pathway **W2** +  $C_2H_4 \rightarrow$  **W2-2** is shown on the left hand side. The [2+2] addition is favored over the [3+2] pathway but both are yielding endothermic products.

For the system **W3** + C<sub>2</sub>H<sub>4</sub>, one [3+2] cycloaddition and two [2+2] cycloadditions are possible. They are presented in Fig. 2. All three cycloaddition pathways are endothermic. The [2+2] addition across the W=NH double bond **W3** + C<sub>2</sub>H<sub>4</sub>  $\rightarrow$  **W3-1** has the lowest barrier and is only slightly endothermic. The other possible [2+2] cycloaddition pathway across the W=O double bond **W3** + C<sub>2</sub>H<sub>4</sub>  $\rightarrow$  **W3-2** is more endothermic and has a higher barrier. Finally, there is the [3+2] pathway **W3** + C<sub>2</sub>H<sub>4</sub>  $\rightarrow$  **W3-3** which has the highest activation barrier and the highest endothermicity of all considered reactions.

The picture changes slightly for ethylene addition to **W4**. The calculated reaction profile is shown in Fig. 3. The [3+2] cycloaddition **W4** +  $C_2H_4 \rightarrow$  **W4-3** is still endothermic and has a high barrier



Fig. 1. Calculated reaction profile for the cycloaddition reactions of ethylene and  $(O=)_2W(CH_3)_2$  (W2) at B3LYP/II//B3LYP/I+ZPE.



**Fig. 2.** Calculated reaction profile for the cycloaddition reactions of ethylene and  $(O=)W(=NH)(CH_3)_2$  (**W3**) at B3LYP/II//B3LYP/I+ZPE.



Fig. 3. Calculated reaction profile for the cycloaddition reactions of ethylene and  $(H_2C=)W(=NH)(CH_3)_2$  (W4) at B3LYP/II//B3LYP/I+ZPE.

but the endothermicity of the process  $W4 + C_2H_4 \rightarrow W4-2$  is comparable to the latter even though the barrier is significantly lower. This implies that the formal W(VI) species W4-2 is energetically nearly degenerate to the W(IV) compound W4-3. The [2+2] cycloaddition across the W=CH<sub>2</sub> double bond  $W4 + C_2H_4 \rightarrow W4-1$  has the lowest barrier and is nearly thermoneutral.

W5 exhibits a different reactivity with olefins which is shown in Fig. 4. The [2+2] cycloaddition  $W5 + C_2H_4 \rightarrow W5-1$  has a low barrier and is slightly exothermic. To the formal [3+2] cycloaddition product W5-1b, no direct transition state was found but it is accessible via the nearly thermoneutral rearrangement  $W5-1 \rightarrow$ W5-1b. Again, we have the situation that the formal W(IV) compound W5-1b is energetically nearly degenerate to formal W(VI) species. Here, the W(VI) compounds are W5 and W5-1. Finally, W5-1 can undergo another rearrangement into another [2+2] cycloaddition product W5-1a. The connectivity of the atoms is the same but W5-1a is slightly lower in energy than W5-1. The associated barrier is negligible. Such a scenario was reported by us also for the system  $W1 + C_2H_4$  [10a].

Fig. 5 shows the calculated cycloadditions for the system **W6** +  $C_2H_4$ . On the left hand side of Fig. 5 the endothermic [3+2] pathway **W6** +  $C_2H_4 \rightarrow$  **W6-2** is shown. It has a rather high barrier. The alternative [2+2] addition of ethylene to **W6** yielding **W6-1** has a significantly lower barrier and a lower endothermicity.



Fig. 4. Calculated reaction profile for the cycloaddition reactions of ethylene and  $(H_2C=)_2W(CH_3)_2$  (W5) at B3LYP/II//B3LYP/I+ZPE.



**Fig. 5.** Calculated reaction profile for the cycloaddition reactions of ethylene and  $(HN=)_2W(CH_3)_2$  (**W6**) at B3LYP/II/B3LYP/I+ZPE.

The studied systems exhibit differences but also similarities in their reactivity with olefins. Table 1 compiles the reaction energies ( $\Delta E_R$ ) and activation energies ( $\Delta E_A$ ) for the possible [2+2] and [3+2] additions of ethylene to **W1–W6**. The favored pathway is indicated by numbers in italics. Note that some of the presented reactions

may involve subsequent rearrangements of the metal compound. In these cases, the highest barrier is given.

Our previously published results [10a] on the system **W1** +  $C_2H_4$  agree best with **W5** +  $C_2H_4$  for the [2+2] cycloaddition across the W=CH<sub>2</sub> double bond. The [2+2] ethylene addition to W5 is predicted to have a slightly lower barrier and to be more exothermic than ethylene addition to W1. The substitution pattern NH/CH<sub>2</sub> seems to enlarge the [2+2]<sub>WC</sub> barrier slightly. Additionally, the slightly exothermic reaction for W1 turns into an endothermic process for W4. The [3+2] cycloaddition of the system  $W1 + C_2H_4$  is quite different from those presented here because it is a pathway where W=O and W=CH<sub>2</sub> double bonds are involved but it is quite similar to  $W3 + C_2H_4$  where the addition involves W=O and W=NH double bonds. In all considered systems W1-W6 the [2+2] addition is clearly favored over the alternative [3+2] pathway. For the similar systems TcO<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>, MnO<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>, RuO<sub>3</sub>CH<sub>2</sub>, OsO<sub>3</sub>CH<sub>2</sub>, OsO<sub>2</sub>(NH)<sub>2</sub>, and MO<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub> (M = Ir, Rh, Co) the reverted preference was observed [3a,6,11-13]. ReO<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub> and MoOCH<sub>2</sub>(CH<sub>3</sub>)<sub>2</sub> on the other side prefer the [2+2] cycloaddition like the six tungsten complexes W1-W6 [9,10b,11].

# 4. Summary

The kinetically favored ethylene addition to **W2** is the [2+2] pathway across the W=O double bond. The barrier is still rather high ( $\Delta E_A$  = 54.5 kcal/mol) and the process is endothermic by 20.9 kcal/mol. For the system **W3** + C<sub>2</sub>H<sub>4</sub>, the [2+2] addition across the W=NH double bond is favored over the alternative cycloadditions although it is still endothermic. The ethylene addition to **W4** clearly favors the [2+2] addition where the W=CH<sub>2</sub> double bond is involved. For the system **W5** + C<sub>2</sub>H<sub>4</sub>, the [2+2] pathway across the W=CH<sub>2</sub> double bond becomes slightly exothermic ( $\Delta E_A$  = -4.6 kcal/mol). The associated barrier is quite small with 7.3 kcal/mol. The activation energy is slightly lower and the exothermicity is slightly higher compared to the system **W1** + C<sub>2</sub>H<sub>4</sub>. The kinetically favored ethylene addition to **W6** is the [2+2]<sub>WN</sub> pathway. The alternative [3+2]<sub>NN</sub> cycloaddition has a higher barrier and also a higher endothermicity.

The presented calculations show that the activation barriers of the favored [2+2] cycloadditions decrease in the order O/O > NH/ NH  $\approx$  O/NH > NH/CH<sub>2</sub>  $\approx$  O/CH<sub>2</sub> > CH<sub>2</sub>/CH<sub>2</sub>. For the reaction energies the order is only slightly different: O/O > NH/NH > O/ NH > NH/CH<sub>2</sub> > O/CH<sub>2</sub>  $\approx$  CH<sub>2</sub>/CH<sub>2</sub>. The preference towards [2+2] or [3+2] cycloaddition depends mainly on the transition metal while the substituents are less important.

#### Table 1

Calculated reaction energies ( $\Delta E_R$ ) and activation energies ( $\Delta E_R$ ) for the cycloaddition reactions of (O=)<sub>2</sub>W(CH<sub>3</sub>)<sub>2</sub> (W2), (O=)W(=NH)(CH<sub>3</sub>)<sub>2</sub> (W3), (HN=)W(=CH<sub>2</sub>)(CH<sub>3</sub>)<sub>2</sub> (W4), (H<sub>2</sub>C=)<sub>2</sub>W(CH<sub>3</sub>)<sub>2</sub> (W5), (HN=)<sub>2</sub>W(CH<sub>3</sub>)<sub>2</sub> (W6) in comparison with the corresponding oxo carbene system (O=)W(=CH<sub>2</sub>)(CH<sub>3</sub>)<sub>2</sub> (W1) at B3LYP/II//B3LYP/I+ZPE. All values are in kcal/mol. The most favorable pathway is given in *italics*.

Cycloaddition	O/CH <sub>2</sub> W1 <sup>a</sup>		0/0 <b>W2</b>		0/NH <b>W3</b>		NH/CH <sub>2</sub> W4		CH <sub>2</sub> /CH <sub>2</sub> <b>W5</b>		NH/NH <b>W6</b>	
	$\Delta E_{\rm R}$	$\Delta E_{A}$	$\Delta E_{\rm R}$	$\Delta E_{A}$	$\Delta E_{\rm R}$	$\Delta E_{A}$	$\Delta E_{\rm R}$	$\Delta E_{A}$	$\Delta E_{\rm R}$	$\Delta E_{A}$	$\Delta E_{\rm R}$	$\Delta E_{A}$
[2+2] <sub>WO</sub>	29.9	33.4	20.9	54.5	26.2	33.8	-	-	-	-	-	-
[2+2] <sub>WN</sub>	-	-	-	-	9.9	29.1	11.3	26.6	-	-	12.3	29.9
[2+2] <sub>WC</sub>	-1.9	9.5 <sup>b</sup>	-	-	-	-	3.8	10.3	-4.6	7.3 <sup>b</sup>	-	-
[3+2] <sub>00</sub>	-	-	68.6	70.7	-	-	-	-	-	-	-	-
[3+2] <sub>ON</sub>	-	-	-	-	47.7	55.5	-	-	-	-	-	-
[3+2] <sub>NN</sub>	-	-	-	-	-	-	-	-	-	-	25.9	47.3
[3+2] <sub>CO</sub>	37.0	52.5	-	-	-	-	-	-	-	-	-	-
[3+2] <sub>CN</sub>	-	-	-	-	-	-	13.9	47.6	-	-	-	-
[3+2] <sub>CC</sub>	-	-	-	-	-	-	-	-	2.3	28.0 <sup>b</sup>	-	-

<sup>a</sup> Values taken from Ref. [8].

<sup>b</sup> Two-step pathway where the highest barrier is given.

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# Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.jorganchem.2009.08.022.

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slightly different from that in Refs. [7,8] and also from that in the present work. Also, the transition states for the reactions  $Os1 + ethylene \rightarrow Os3a$  and  $Os1 + ethylene \rightarrow Os3b$  were only found after publication of this work. They are reported in Ref. [7].

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